

Prof. Dr. Alfred Toth

Vollständige eigenreale Thematisation

1. In Toth (2026) hatten wir gezeigt, daß man die strukturellen Realitäten der 27 Dualsysteme des vollständigen ternären semiotischen Systems in einer Tripelrelation der folgenden Form notieren kann

$$(X, Y) \rightarrow Z$$

$$X \rightarrow Y \leftarrow Z$$

$$X \leftarrow (Y, Z).$$

Wir hatten aber bisher die sog. eigenrealen Dualsysteme mit ternären strukturellen Realitäten ausgespart, die bekanntlich dreifache Thematisierungsmöglichkeiten bieten.

2. Vollständige eigenreale Thematisation

$$3.1 \quad 2.2 \quad 1.3 \quad \times \quad 3.1 \quad 2.2 \quad 1.3 \quad (3.1, 2.2) \rightarrow 1.3$$

$$3.1 \rightarrow 2.2 \leftarrow 1.3$$

$$3.1 \leftarrow (2.2, 1.3)$$

$$3.1 \quad 1.3 \quad 2.2 \quad \times \quad 2.2 \quad 3.1 \quad 1.3 \quad (2.2, 3.1) \rightarrow 1.3$$

$$2.2 \rightarrow 3.1 \leftarrow 1.3$$

$$2.2 \leftarrow (3.1, 1.3)$$

$$2.2 \quad 3.1 \quad 1.3 \quad \times \quad 3.1 \quad 1.3 \quad 2.2 \quad (3.1, 1.3) \rightarrow 2.2$$

$$3.1 \rightarrow 1.3 \leftarrow 2.2$$

$$3.1 \leftarrow (1.3, 2.2)$$

$$2.2 \quad 1.3 \quad 3.1 \quad \times \quad 1.3 \quad 3.1 \quad 2.2 \quad (1.3, 3.1) \rightarrow 2.2$$

$$1.3 \rightarrow 3.1 \leftarrow 2.2$$

$$1.3 \leftarrow (3.1, 2.2)$$

$$1.3 \quad 3.1 \quad 2.2 \quad \times \quad 2.2 \quad 1.3 \quad 3.1 \quad (2.2, 1.3) \rightarrow 3.1$$

$$2.2 \rightarrow 1.3 \leftarrow 3.1$$

$$2.2 \leftarrow (1.3, 3.1)$$

$$1.3 \quad 2.2 \quad 3.1 \quad \times \quad 1.3 \quad 2.2 \quad 3.1 \quad (1.3, 2.2) \rightarrow 3.1$$

$$1.3 \rightarrow 2.2 \leftarrow 3.1$$

$$1.3 \leftarrow (2.2, 3.1)$$

$$\begin{array}{ccccccc} 3.1 & 2.3 & 1.2 & \times & 2.1 & 3.2 & 1.3 \\ & & & & & & (2.1, 3.2) \rightarrow 1.3 \\ & & & & & & 2.1 \rightarrow 3.2 \leftarrow 1.3 \\ & & & & & & 2.1 \leftarrow (3.2, 1.3) \end{array}$$

$$\begin{array}{ccccccc} 3.1 & 1.2 & 2.3 & \times & 3.2 & 2.1 & 1.3 \\ & & & & & & (3.2, 2.1) \rightarrow 1.3 \\ & & & & & & 3.2 \rightarrow 2.1 \leftarrow 1.3 \\ & & & & & & 3.2 \leftarrow (2.1, 1.3) \end{array}$$

$$\begin{array}{ccccccc} 2.3 & 3.1 & 1.2 & \times & 2.1 & 1.3 & 3.2 \\ & & & & & & (2.1, 1.3) \rightarrow 3.2 \\ & & & & & & 2.1 \rightarrow 1.3 \leftarrow 3.2 \\ & & & & & & 2.1 \leftarrow (1.3, 3.2) \end{array}$$

$$\begin{array}{ccccccc} 2.3 & 1.2 & 3.1 & \times & 1.3 & 2.1 & 3.2 \\ & & & & & & (1.3, 2.1) \rightarrow 3.2 \\ & & & & & & 1.3 \rightarrow 2.1 \leftarrow 3.2 \\ & & & & & & 1.3 \leftarrow (2.1, 3.2) \end{array}$$

$$\begin{array}{ccccccc} 1.2 & 3.1 & 2.3 & \times & 3.2 & 1.3 & 2.1 \\ & & & & & & (3.2, 1.3) \rightarrow 2.1 \\ & & & & & & 3.2 \rightarrow 1.3 \leftarrow 2.1 \\ & & & & & & 3.2 \leftarrow (1.3, 2.1) \end{array}$$

$$\begin{array}{ccccccc} 1.2 & 2.3 & 3.1 & \times & 1.3 & 3.2 & 2.1 \\ & & & & & & (1.3, 3.2) \rightarrow 2.1 \\ & & & & & & 1.3 \rightarrow 3.2 \leftarrow 2.1 \\ & & & & & & 1.3 \leftarrow (3.2, 2.1) \end{array}$$

$$\begin{array}{ccccccc} 3.2 & 2.1 & 1.3 & \times & 3.1 & 1.2 & 2.3 \\ & & & & & & (3.1, 1.2) \rightarrow 2.3 \\ & & & & & & 3.1 \rightarrow 1.2 \leftarrow 2.3 \\ & & & & & & 3.1 \leftarrow (1.2, 2.3) \end{array}$$

$$\begin{array}{ccccccc} 3.2 & 1.3 & 2.1 & \times & 1.2 & 3.1 & 2.3 \\ & & & & & & (1.2, 3.1) \rightarrow 2.3 \\ & & & & & & 1.2 \rightarrow 3.1 \leftarrow 2.3 \\ & & & & & & 1.2 \leftarrow (3.1, 2.3) \end{array}$$

2.1	3.2	1.3	×	3.1	2.3	1.2	(3.1, 2.3) → 1.2 3.1 → 2.3 ← 1.2 3.1 ← (2.3, 1.2)
2.1	1.3	3.2	×	2.3	3.1	1.2	(2.3, 3.1) → 1.2 2.3 → 3.1 ← 1.2 2.3 ← (3.1, 1.2)
1.3	3.2	2.1	×	1.2	2.3	3.1	(1.2, 2.3) → 3.1 1.2 → 2.3 → 3.1 1.2 ← (2.3, 3.1)
1.3	2.1	3.2	×	2.3	1.2	3.1	(2.3, 1.2) → 3.1 2.3 → 1.2 ← 3.1 2.3 ← (1.2, 3.1)
3.2	2.3	1.1	×	1.1	3.2	2.3	(1.1, 3.2) → 2.3 1.1 → 3.2 ← 2.3 1.1 ← (3.2, 2.3)
3.2	1.1	2.3	×	3.2	1.1	2.3	(3.2, 1.1) → 2.3 3.2 → 1.1 ← 2.3 3.2 ← (1.1, 2.3)
2.3	3.2	1.1	×	1.1	2.3	3.2	(1.1, 2.3) → 3.2 1.1 → 2.3 ← 3.2 1.1 ← (2.3, 3.2)
2.3	1.1	3.2	×	2.3	1.1	3.2	(2.3, 1.1) → 3.2 2.3 → 1.1 ← 3.2 2.3 ← (1.1, 3.2)
1.1	3.2	2.3	×	3.2	2.3	1.1	(3.2, 2.3) → 1.1 3.2 → 2.3 ← 1.1

							$3.2 \leftarrow (2.3, 1.1)$
1.1	2.3	3.2	×	2.3	3.2	1.1	$(2.3, 3.2) \rightarrow 1.1$
							$2.3 \rightarrow 3.2 \leftarrow 1.1$
							$2.3 \leftarrow (3.2, 1.1)$
3.3	2.1	1.2	×	2.1	1.2	3.3	$(2.1, 1.2) \rightarrow 3.3$
							$2.1 \rightarrow 1.2 \leftarrow 3.3$
							$2.1 \leftarrow (1.2, 3.3)$
3.3	1.2	2.1	×	1.2	2.1	3.3	$(1.2, 2.1) \rightarrow 3.3$
							$1.2 \rightarrow 2.1 \leftarrow 3.3$
							$1.2 \leftarrow (2.1, 3.3)$
2.1	3.3	1.2	×	2.1	3.3	1.2	$(2.1, 3.3) \rightarrow 1.2$
							$2.1 \rightarrow 3.3 \leftarrow 1.2$
							$2.1 \leftarrow (3.3, 1.2)$
2.1	1.2	3.3	×	3.3	2.1	1.2	$(3.3, 2.1) \rightarrow 1.2$
							$3.3 \rightarrow 2.1 \leftarrow 1.2$
							$3.3 \leftarrow (2.1, 1.2)$
1.2	3.3	2.1	×	1.2	3.3	2.1	$(1.2, 3.3) \rightarrow 2.1$
							$1.2 \rightarrow 3.3 \leftarrow 2.1$
							$1.2 \leftarrow (3.3, 2.1)$
1.2	2.1	3.3	×	3.3	1.2	2.1	$(3.3, 1.2) \rightarrow 2.1$
							$3.3 \rightarrow 1.2 \leftarrow 2.1$
							$3.3 \leftarrow (1.2, 2.1)$
3.3	2.2	1.1	×	1.1	2.2	3.3	$(1.1, 2.2) \rightarrow 3.3$
							$1.1 \rightarrow 2.2 \leftarrow 3.3$
							$1.1 \leftarrow (2.2, 3.3)$

3.3	1.1	2.2	×	2.2	1.1	3.3	(2.2, 1.1) → 3.3 2.2 → 1.1 ← 3.3 2.2 ← (1.1, 3.3)
2.2	3.3	1.1	×	1.1	3.3	2.2	(1.1, 3.3) → 2.2 1.1 → 3.3 ← 2.2 1.1 ← (3.3, 2.2)
2.2	1.1	3.3	×	3.3	1.1	2.2	(3.3, 1.1) → 2.2 3.3 → 1.1 ← 2.2 3.3 ← (1.1, 2.2)
1.1	3.3	2.2	×	2.2	3.3	1.1	(2.2, 3.3) → 1.1 2.2 → 3.3 ← 1.1 2.2 ← (3.3, 1.1)
1.1	2.2	3.3	×	3.3	2.2	1.1	(3.3, 2.2) → 1.1 3.3 → 2.2 ← 1.1 3.3 ← (2.2, 1.1)

Literatur

Toth, Alfred, Vollständige Thematisierungstripel. In: Electronic Journal for Mathematical Semiotics, 2026

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